# Reversible Diels-Alder Addition to Fullerenes: A Study of Equilibria Using ${ }^{3} \mathrm{He}$ NMR Spectroscopy 

Guan-Wu Wang, ${ }^{\dagger}$ Martin Saunders,* and R. James Cross*<br>Contribution from the Department of Chemistry, Yale University, New Haven, Connecticut 06520-8107

Received April 18, 2000. Revised Manuscript Received October 31, 2000


#### Abstract

He}\) NMR spectroscopy has been used to study the equilibria of Diels-Alder additions of 9,10dimethyl anthracene (DMA) to ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ and ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$. Spectra of a series of equilibrium mixtures showed peaks for the isomeric adducts. One monoadduct, six bis-adducts, eleven tris-adducts, and ten tetrakis-adducts of DMA to $\mathrm{C}_{60}$ were seen. One monoadduct and three bis-adducts of $\mathrm{C}_{70}$ were detected. Equilibrium constants were found for these reactions and values for $\Delta G, \Delta H$, and $\Delta S$ were obtained.


## Introduction

$\mathrm{C}_{60}$ and other fullerenes are quite reactive. ${ }^{1-3}$ Most reactions result in irreversible addition to yield mixtures of mono- and multiple adducts. However, the Diels-Alder reaction of 9,10dimethylanthracene (DMA) with $\mathrm{C}_{60}$ (see Figure 1) has been shown by Hirsch et al. to be reversible at room temperature, yielding mixtures of isomers of $\mathrm{C}_{60}(\mathrm{DMA})_{n} .{ }^{4}$ DMA behaves in a similar manner toward $\mathrm{C}_{70}$. These reactions are of interest because the equilibrium quantities of the regioisomers can yield thermodynamic information about these compounds. How can one study these equilibria? We have shown that ${ }^{3} \mathrm{He}$ NMR is a very powerful tool for studying fullerene reactions. ${ }^{5,6}$ Each ${ }^{3} \mathrm{He}$-labeled fullerene and fullerene derivative gives a distinct, sharp ${ }^{3} \mathrm{He}$ NMR peak. In this paper, we report the use of ${ }^{3} \mathrm{He}$ NMR to determine the number of addends, equilibrium constants, $\Delta G, \Delta H$, and $\Delta S$ for $\mathrm{C}_{60}(\mathrm{DMA})_{n}$ and $\mathrm{C}_{70}(\mathrm{DMA})_{n}$. We believe that ${ }^{3} \mathrm{He}$ inside fullerenes has a negligible effect on rates and equilibrium constants for reactions. In all cases where the same reactions have been studied using ${ }^{3} \mathrm{He}$ NMR and using other methods, the same results have been obtained.

With reactions that add across 6,6 fusions, only one monoadduct of $\mathrm{C}_{60}$ is formed. There are eight possible regioisomers for bis-addition of a symmetric addend, and there is a case ${ }^{7}$ where all of them have been separated and characterized. Nine regioisomers ${ }^{8}$ of $\mathrm{C}_{60}$ bis-adducts have been separated when the

[^0]

Figure 1. The monoadduct of 9,10 -dimethylanthracene and $\mathrm{C}_{60}$. The figure was made using GaussView 2.1.
second addend is different from the first. Separation of the individual isomers of tris- and higher adducts is difficult. Characterization of only a few of them ${ }^{9,10}$ have been reported. Recently Hirsch's group has isolated seven regioisomers ${ }^{11}$ out

[^1]of 46 possible tris-adducts of Bingel reaction products of $\mathrm{C}_{60}$. The chemistry of $\mathrm{C}_{70}$ is potentially more complex than that of $\mathrm{C}_{60}$ due to the lower symmetry of $\mathrm{C}_{70}$. Four monoadducts from the reaction mixture of $\mathrm{C}_{70}$ and benzyne have been separated, ${ }^{12}$ and some examples of bis- up to octakis-adducts have been reported. ${ }^{3,13}$ However, the determination of the maximum number of the tris-adducts and higher adduct isomers of $\mathrm{C}_{60}$ and $\mathrm{C}_{70}$ formed in a reaction remains a challenging task.

## Experimental Section

${ }^{3} \mathrm{He}$-labeled fullerenes were prepared by using our high-temperature and high-pressure procedure. ${ }^{14} \mathrm{C}_{60}$ and $\mathrm{C}_{70}$ were labeled with ${ }^{3} \mathrm{He}$ six times and twice, respectively, to get more ${ }^{3} \mathrm{He}$ into the cages of fullerenes and thus obtain much better signal-to-noise ratios in the ${ }^{3} \mathrm{He}$ NMR spectra. All ${ }^{3} \mathrm{He}$ NMR samples were prepared directly in NMR tubes. A weighed amount of DMA and ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}(7.20 \mathrm{mg})$ or ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$ $(4.20 \mathrm{mg})$ and 1 mg of $\mathrm{Cr}(\mathrm{acac})_{3}$ were put in a NMR tube and dissolved in 4:1 1-methylnaphthalene $/ \mathrm{CD}_{2} \mathrm{Cl}_{2}(\sim 0.4 \mathrm{~mL})$. First, $\sim 0.5$ equiv of DMA was added. The mixture was allowed to stand long enough (overnight) ${ }^{15}$ to reach the equilibrium, and its ${ }^{3} \mathrm{He}$ NMR spectrum was taken. Then a weighed amount of DMA was added to the above mixture to get another sample. This procedure could be repeated many times until a saturated solution was reached. About 15 equiv of DMA can be added to ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ and 1 equiv of DMA to ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$ with no precipitation. For the variable-temperature experiments, the samples were equilibrated for at least 1 h in the probe before an acquisition was started. A mixture of $3.60 \mathrm{mg}{ }^{3} \mathrm{He} @ \mathrm{C}_{60}, 4.20 \mathrm{mg}$ of ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$, 1.55 mg of DMA ( 0.75 equiv), and 1 mg of $\mathrm{Cr}(\mathrm{acac})_{3}$ was prepared in 0.4 mL of $4: 1$ 1-methylnaphthalene $/ \mathrm{CD}_{2} \mathrm{Cl}_{2}$ to get the ratio of the equilibrium constants for $\mathrm{C}_{60}$ with DMA versus $\mathrm{C}_{70}$ with DMA from the ${ }^{3} \mathrm{He}$ NMR. All ${ }^{3} \mathrm{He}$ NMR spectra were taken at 381 MHz on a Bruker AM-500 NMR spectrometer with ${ }^{3} \mathrm{He}$ dissolved in the solution as reference. No pulse delay was used, and a line-broadening of 2 Hz was applied.

## Results and Discussion

The Diels-Alder addition of DMA to $\mathrm{C}_{60}$ is reversible at ambient temperatures, and gives, successively, mono-, bis-, tris-, and tetrakis-adducts with increasing DMA concentration. As more DMA is added, larger amounts of higher adducts are formed. A series of mixtures of DMA and ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ was prepared in 4:1 1-methylnaphthalene/ $\mathrm{CD}_{2} \mathrm{Cl}_{2}$. After the equilibrium was established, the ${ }^{3} \mathrm{He}$ NMR spectra were recorded. With few exceptions, each line in the ${ }^{3} \mathrm{He}$ NMR spectra is well resolved and corresponds to a distinct fullerene adduct. Two
(10) (a) Fagan, P. J.; Calabrese, J. L.; Malone, B. J. Am. Chem. Soc. 1991, 113, 9408-9409. (b) Hirsch, A.; Lamparth, I.; Grsser, T.; Karfunkel, H. R. J. Am. Chem. Soc. 1994, 116, 9385-9386. (c) Kräutler, B.; Maynollo, J. Angew. Chem., Int. Ed. Engl. 1995, 34, 87-88. (d) Bouldon, C.; Gisselbrecht, J.-P.; Gross, M.; Issacs, L.; Anderson, H. L.; Faust, R.; Diederich, F. Helv. Chim. Acta 1995, 78, 1334-1344. (e) Haldimann, R. F.; Klaerner, F.-G.; Diederich, F. Chem. Commun. 1997, 237-238. (f) Schick, G.; Levitus, M.; Kvetko, L.; Johnson, B. A.; Lamparth, I.; Lunkwitz, R.; Ma, B.; Khan, S. I.; Garcia-Garibay, M. A.; Rubin, Y. J. Am. Chem. Soc. 1999, 121, 3246-3247.
(11) Djojo, F.; Hirsch, A.; Grimme, S. Eur. J. Org. Chem. 1999, 30273039.
(12) Meier, M. S.; Wang, G.-W.; Haddon, R. C.; Brock, C. P.; Lloyd, M. A.; Selegue, J. P. J. Am. Chem. Soc. 1998, 120, 2337-2342.
(13) (a) Thilgen, C.; Herrmann, A.; Diederich, F. Angew. Chem., Int. Ed. Engl. 1997, 36, 2269-2280 and references therein. (b) Spielmann, H. P.; Wang, G.-W.; Meier, M. S.; Weedon, B. R. J. Org. Chem. 1998, 63, 9865-9871. (c) Herrmann, A.; Ruttimann, M. W.; Gibtner, T.; Thilgen, C.; Diederich, F.; Mordasini, T.; Thiel, W. Helv. Chim. Acta 1999, 82, 261-289.
(14) Saunders, M.; Jiménez-Vázquez, H. A.; Cross, R. J.; Mroczkowski, S.; Freedberg, D. I.; Anet, A. L. Nature 1994, 367, 256-258.
(15) 7.20 mg of $\mathrm{C}_{60}$ and 2.06 mg of DMA (1 equiv) were mixed in 0.5 mL of ODCB- $d_{4} .{ }^{1} \mathrm{H}$ NMR was used to follow the reaction of $\mathrm{C}_{60}$ and DMA. It was found that almost no free DMA could be found by ${ }^{1} \mathrm{H}$ NMR $\sim 30 \mathrm{~min}$. after the mixing.


Figure 2. ${ }^{3} \mathrm{He}$ NMR spectra of ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ with (a) 2.5 equiv of DMA and (b) 10 equiv of DMA at room temperature. The numbers $\mathbf{1}, \mathbf{2}, \mathbf{3}$, 4 stand for the isomers of mono-, bis-, tris-, and tetrakis-adducts, respectively.

Table 1. Chemical Shifts and Fractional Concentrations for the Reaction of $\mathrm{C}_{60}$ and DMA at 295.4 K

|  | $\delta^{a}$ | $\mathrm{F}^{\text {b }}$ |  | $\delta^{a}$ | $\mathrm{F}^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mono |  |  | Tetrakis |  |
|  | -9.77 | 1.000 | 1 | -11.08 | 0.012 |
|  | Bis |  | 2 | -12.77 | 0.011 |
| 1 | -8.95 | 0.006 | 3 | -13.70 | 0.026 |
| 2 | -10.44 | 0.060 | 4 | -14.52 | 0.045 |
| 3 | -10.66 | 0.008 | 5 | -14.57 | 0.280 |
| 4 | -11.29 | 0.087 | 6 | -14.60 | 0.367 |
| 5 | -12.83 | 0.448 | 7 | -14.79 | 0.037 |
| 6 | $-12.84$ | 0.392 | 8 | -15.26 | 0.027 |
|  |  |  | 9 | -15.30 | 0.168 |
|  |  |  | 10 | -15.47 | 0.027 |

Tris

| 1 | -10.93 | 0.008 |
| ---: | ---: | ---: |
| 2 | -11.42 | 0.014 |
| 3 | -11.43 | 0.028 |
| 4 | -11.54 | 0.021 |
| 5 | -12.08 | 0.008 |
| 6 | -13.42 | 0.068 |
| 7 | -13.50 | 0.157 |
| 8 | -13.65 | 0.020 |
| 9 | -14.21 | 0.217 |
| 10 | -15.44 | 0.067 |
| 11 | -16.14 | 0.390 |

[^2]representative ${ }^{3} \mathrm{He}$ NMR spectra of ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ with 2.5 equiv and 10 equiv of DMA are shown in Figure 2.

The assignment of a given NMR peak to the number of DMA addends is straightforward. If the ratio of NMR intensities of two peaks is independent of DMA concentration, then the two peaks correspond to adducts with the same number of DMA molecules. If the ratio changes with DMA concentration, the peak that increases more rapidly corresponds to an adduct with more DMA molecules. The 29 distinct ${ }^{3} \mathrm{He}$ peaks seen were assigned in this way. We found one monoadduct, six bis-adducts, eleven tris-adducts, and ten tetrakis-adducts. We have seen no evidence of pentakis- or hexakis-adducts even at the highest concentrations of DMA available to us. The amount of any single higher adduct is evidently too low for us to detect. Table 1 lists the isomers, their ${ }^{3} \mathrm{He}$ NMR shifts, and the fraction of the NMR intensity for each isomer at 295.4 K . Figure 3 shows distributions of $\mathrm{C}_{60}$, monoadduct, and the


Figure 3. Distributions of $\mathrm{C}_{60}$ and $\mathrm{C}_{60}(\mathrm{DMA})_{n}$ at different ratios of DMA/C ${ }_{60}$. ( $\bullet$ ) $\mathrm{C}_{60} ;(\mathbf{\Delta})$ monoadduct; ( $\boldsymbol{\bullet}$ ) bis-adducts; $(\boldsymbol{\bullet})$ tris-adducts; ( $\mathbf{\nabla})$ tetrakis-adducts. The curves $(--) \mathrm{C}_{60} ;(---)$ monoadduct; $(\cdots)$ bis-adducts; $(\cdots-\cdots \cdot \cdot)$ tris-adducts; ( --- ) tetrakis-adducts) are the calculated curves by inputting the $K_{1}, K_{2}, K_{3}, K_{4}$ as $3634,496,41.7$, $2.36 \mathrm{M}^{-1}$, and the concentration of $\mathrm{C}_{60}$ as 0.025 M .
sums of bis-, tris- and tetrakis-addducts at different ratios of DMA/C 60 .

We assumed the reversible reactions of ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ and DMA as shown in eqs $1-4$ :

$$
\begin{gather*}
{ }^{3} \mathrm{He} @ \mathrm{C}_{60}+\mathrm{DMA} \stackrel{K_{1}}{\leftrightharpoons}{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})  \tag{1}\\
{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})+\mathrm{DMA} \stackrel{K_{2}}{\leftrightharpoons}{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})_{2}  \tag{2}\\
{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})_{2}+\mathrm{DMA} \stackrel{K_{3}}{\leftrightharpoons}{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})_{3}  \tag{3}\\
{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})_{3}+\mathrm{DMA} \stackrel{K_{4}}{\leftrightharpoons}{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})_{4} \tag{4}
\end{gather*}
$$

The quantities considered in these equations are the sums of all bis-, tris- and tetrakis-adducts. While the relative amounts of $\mathrm{C}_{60}$ and the mono-, bis-, tris- and tetrakis-adducts are observable by using the ${ }^{3} \mathrm{He}$ spectra, the amount of free DMA is not directly observable in the ${ }^{3} \mathrm{He}$ spectrum. Therefore, a computer program was written which uses the concentration of free DMA as a parameter in simulating the experimental results. For any set of assumed values of $K_{1}, K_{2}, K_{3}, K_{4}$, a series of values for concentrations of free $\mathrm{C}_{60}$ and free DMA was generated. From these values, the sums of the concentrations of the different kinds of adducts could be generated using the above equations. Adding these concentrations generates values for the total concentration of $\mathrm{C}_{60}$. Total DMA was calculated by addition weighted by the number of DMA molecules on each adduct. These calculated values could then be compared with the experimental values. $K_{1}, K_{2}, K_{3}$, and $K_{4}$ were adjusted to fit the experimental points. Values of $3600,490,41,2.3 \mathrm{M}^{-1}$ were found to best fit the experimental data and yielded the theoretical concentration curves shown in Figure 3. As can be seen, all of the experimental points for the fractions of $\mathrm{C}_{60}$ and $\mathrm{C}_{60}(\mathrm{DMA})_{n}$ at different DMA/C 60 ratios are very near to the calculated curves. The concentration of free $\mathrm{C}_{60}$ decreases with added DMA and is near zero at 2 equiv of DMA, while those of the mono-, bis- and tris-adducts first increase and reach a maximum and then decrease. The concentration of tris-adduct reaches its

Table 2. Peak Intensities, Equilibrium Constants $K$, and Free Energies $\Delta G$ of $\mathrm{C}_{60}+n \mathrm{DMA} \leftrightarrows \mathrm{C}_{60}(\mathrm{DMA})_{n}{ }^{a}$

| $T(\mathrm{~K})$ | 295.4 | 305.0 | 315.0 | 325.0 |
| :--- | :---: | :---: | :---: | :---: |
| $\mathrm{C}_{60}$ | 17.66 | 14.49 | 6.21 | 14.30 |
| mono | 39.32 | 26.81 | 8.83 | 13.89 |
| bis 2 | 0.84 | 0.69 |  |  |
| bis 4 | 1.09 | 0.94 |  |  |
| bis 5 | 5.65 | 3.65 | 0.94 | 1.37 |
| bis 6 | 4.70 | 3.21 | 0.74 | 0.92 |
| bis total | 12.27 | 8.49 | 1.68 | 2.29 |
| $\mathrm{C}_{\mathrm{DMA}^{\prime}(\mathrm{mM})^{b}}$ | 0.617 | 1.688 | 5.448 | 8.526 |
| $K_{1}\left(\mathrm{M}^{-1}\right)$ | 3600 | 1100 | 260 | 110 |
| $K_{2}\left(\mathrm{M}^{-1}\right)$ | 510 | 190 | 35 | 19 |
| $\Delta G_{1}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | -4.8 | -4.2 | -3.5 | -3.1 |
| $\Delta G_{2}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | -3.7 | -3.2 | -2.2 | -1.9 |

${ }^{a}$ The initial (unreacted) concentrations are $\mathrm{C}_{60}: 25.0 \mathrm{mM}$, DMA: $23.7 \mathrm{mM} .{ }^{b}$ The concentration of free DMA obtained by subtracting the amount of bound DMA from the initial concentration.


Figure 4. The plots of $\ln K$ vs $T^{-1}$ for the first two equilibria of the reaction of $\mathrm{C}_{60}$ with DMA. ( ) $K_{1}$; ( $\left.\mathbf{(}\right) K_{2}$.

Table 3. Chemical Shifts and Fractional Concentrations for the Reaction of $\mathrm{C}_{70}$ and DMA at 295.4 K

|  | $\delta^{a}$ | $\mathrm{~F}^{b}$ |
| :---: | :---: | :---: |
| 1 | $\mathrm{C}_{70}$ |  |
|  | -28.80 | 1.000 |
| 1 | Mono |  |
|  | -26.93 | 1.000 |
| 1 | Bis | 0.389 |
| 2 | -24.73 | 0.139 |
| 3 | -24.67 | 0.472 |

${ }^{a}$ Chemical shift in ppm relative to dissolved ${ }^{3} \mathrm{He}$ gas. ${ }^{b}$ Fraction in each isomer of the total NMR signal for all isomers with a given number of DMA addends.
maximum at $\sim 6$ equiv of DMA and then decreases slowly. The concentration of tetrakis-adducts is still going up.

It was also possible to derive equations for obtaining the equilibrium constants directly from the experimental data without using the simulation process described above. Knowing the initial amounts of $\mathrm{C}_{60}$ and DMA and the relative amounts of each product, one can calculate the concentration of free DMA by subtracting the concentrations of the adducts. The resulting equilibrium constants were similar to those obtained by the simulation method.

The highest field helium peak of the tris-adducts is shifted further upfield than the highest field peak of the bis-adducts, but the highest field peak of the tetrakis-adducts is not as far upfield. The magnetic field inside the $\mathrm{C}_{60}$ cage changes with both the number of added groups and the addition patterns. The

Table 4. Peak Intensities, Equilibrium Constants $K$, and Free Energies $\Delta G$ of $\mathrm{C}_{70}+n \mathrm{DMA} \leftrightarrows \mathrm{C}_{70}(\mathrm{DMA})_{n}{ }^{a}$

| $T(\mathrm{~K})$ | 295.4 | 305.0 | 315.0 | 325.0 |
| :--- | ---: | :---: | :---: | :---: |
| $\mathrm{C}_{70}$ | 104.79 | 304.24 | 52.30 | 32.90 |
| mono | 59.05 | 122.41 | 12.72 | 4.34 |
| bis 1 | 1.56 | 2.34 |  |  |
| bis 2 | 0.32 | 0.71 |  |  |
| bis 3 | 1.83 | 2.68 |  |  |
| bis total | 3.71 | 5.73 |  |  |
| $\mathrm{C}_{\mathrm{DMA}^{\prime}(\mathrm{mM})^{b}}$ | 0.7539 | 1.964 | 3.547 | 4.645 |
| $K_{1}\left(\mathrm{M}^{-1}\right)$ | 750 | 210 | 69 | 28 |
| $K_{2}\left(\mathrm{M}^{-1}\right)$ | 83 | 24 |  |  |
| $\Delta G_{1}\left(\mathrm{kcal} \mathrm{mol}^{-1}\right)$ | -3.9 | -3.2 | -2.7 | -2.2 |
| $\Delta G_{2}(\mathrm{kcal} \mathrm{mol}$ |  |  |  |  |

${ }^{a}$ The initial (unreacted) concentrations are $\mathrm{C}_{70}: 13.9 \mathrm{mM}$, DMA: $6.26 \mathrm{mM} .{ }^{b}$ The concentration of free DMA obtained by subtracting the amount of bound DMA from the initial concentration.
number of $\mathrm{C}_{60}(\mathrm{DMA})_{n}$ isomers seen increases from one for the monoadduct, six for the bis-adducts, eleven for tris-adducts and then decreases to ten for tetrakis-adducts. Furthermore, the numbers of major isomers increase first and then decrease, one for monoadduct, four for bis-adducts, four for tris-adducts, and three for tetrakis-adducts. The addition of DMA to $\mathrm{C}_{60}$ seems to be more selective at later stages.

Elevated temperature drives the equilibrium back toward free $\mathrm{C}_{60} \cdot{ }^{3} \mathrm{He}$ NMR spectra of a fixed amount of ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ and DMA were obtained at different temperatures (from 295.4 to 325 K ). These data allow the calculation of the equilibrium constants $K$ and free energies $\Delta G$. Table 2 lists these results along with the peak intensities at different temperatures.

Assuming $\Delta H$ does not change over our temperature range $\left(30^{\circ} \mathrm{C}\right)$, applying the van't Hoff equation gives:

$$
\begin{equation*}
\frac{\mathrm{d}(\ln K)}{\mathrm{d}(1 / T)}=-\frac{\Delta H}{R} \tag{5}
\end{equation*}
$$

The slope of the graph of $\ln K$ vs $T^{-1}$ multiplied by $-R$ gives $\Delta H$. Figure 4 shows the plots of $\ln K$ vs $T^{-1}$ for the first two equilibria of the reaction of $\mathrm{C}_{60}$ with DMA. A least-squares fit gives $\Delta H_{1}$ as $-22.9 \mathrm{kcal} \mathrm{mol}^{-1}$ for $\mathrm{C}_{60}+\mathrm{DMA} \leftrightarrows \mathrm{C}_{60}(\mathrm{DMA})$, and $\Delta H_{2}$ as $-22.5 \mathrm{kcal} \mathrm{mol}^{-1}$ for $\mathrm{C}_{60}(\mathrm{DMA})+\mathrm{DMA} \leftrightarrows$ $\mathrm{C}_{60}(\mathrm{DMA})_{2} . \Delta S$ can be calculated from

$$
\begin{equation*}
\Delta G=\Delta H-T \Delta S \tag{6}
\end{equation*}
$$

$\Delta S_{1}$ and $\Delta S_{2}$ are -61.2 and $-63.7 \mathrm{cal} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$, respectively.
In the same way, we obtained the number of isomers and equilibrium constants for the reaction of ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$ and DMA. Unfortunately, the solubility of $\mathrm{C}_{70}(\mathrm{DMA})_{n}$ is much lower than that of $\mathrm{C}_{60}(\mathrm{DMA})_{n}$. When the DMA concentration is higher than 1.5 equivalent in $14 \mathrm{mM} \mathrm{C} 7_{70}, \mathrm{C}_{70}(\mathrm{DMA})_{n}$ started to precipitate out. We found only one monoadduct ${ }^{16}$ and three bis-adducts in the equilibrium reaction mixtures. The chemical shifts and equilibrium fractions are given in Table 3. The equilibrium constants and $\Delta G$ s are listed in Table 4.

[^3]

Figure 5. The plot of $\ln K_{1}$ vs $T^{-1}$ for the first equilibrium of the reaction of $\mathrm{C}_{70}$ with DMA.

The plot of $\ln K_{1}$ vs $T^{-1}$ for $\mathrm{C}_{70}+\mathrm{DMA} \leftrightarrows \mathrm{C}_{70}(\mathrm{DMA})$ is shown in Figure 5. The same treatment as for $\mathrm{C}_{60}$ gives $\Delta H_{1}$ and $\Delta S_{1}$ as $-21.1 \mathrm{kcal} \mathrm{mol}^{-1}$ and $-58.5 \mathrm{cal} \mathrm{mol}^{-1} \mathrm{~K}^{-1} . \Delta H_{1}$ and $\Delta S_{1}$ values for the reaction of $\mathrm{C}_{70}$ with DMA are very close to those of $\Delta H_{1}$ and $\Delta S_{1}$ and $\Delta H_{2}$ and $\Delta S_{2}$ for the reaction of $\mathrm{C}_{60}$ and DMA. This is reasonable because both $\mathrm{C}_{60}$ and $\mathrm{C}_{70}$ involve same type of reacting double bond and same reagent DMA in the Diels-Alder reactions.

We have also run the ${ }^{3} \mathrm{He} \mathrm{NMR}$ spectrum of a mixture of ${ }^{3} \mathrm{He} @ \mathrm{C}_{60},{ }^{3} \mathrm{He} @ \mathrm{C}_{70}$, and DMA to determine the relative equilibrium constants. The ratio $K_{1}\left(\mathrm{C}_{60}\right) / K_{1}\left(\mathrm{C}_{70}\right)$ of the first equilibrium for the reactions of DMA with $\mathrm{C}_{60}$ and $\mathrm{C}_{70}$ is

$$
\begin{equation*}
\frac{K_{1}\left(\mathrm{C}_{60}\right)}{K_{1}\left(\mathrm{C}_{70}\right)}=\left[\frac{{ }^{3} \mathrm{He} @ \mathrm{C}_{60}(\mathrm{DMA})}{{ }^{3} \mathrm{He} @ \mathrm{C}_{70}(\mathrm{DMA})}\right] \times\left[\frac{{ }^{3} \mathrm{He} @ \mathrm{C}_{70}}{{ }^{3} \mathrm{He} @ \mathrm{C}_{60}}\right] \tag{7}
\end{equation*}
$$

The ratio $K_{1}\left(\mathrm{C}_{60}\right) / K_{1}\left(\mathrm{C}_{70}\right)$ is 4.65 , very close to the ratio of 4.83 ( $3608 \mathrm{M}^{-1} / 747 \mathrm{M}^{-1}$ ) obtained from the separate experiments.

We have tried to react ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ with 9,10-diphenylanthracene (DPA), but only the sharp peak of ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ could be observed after an overnight ${ }^{3} \mathrm{He}$ NMR run. The reaction of DPA with $\mathrm{C}_{60}$ seems to be much less favorable. Studies on the reactions of fullerenes with other anthracene derivatives are underway.

## Conclusions

We have utilized ${ }^{3} \mathrm{He}$ NMR spectroscopy to study the equilibria of the reactions of $\mathrm{C}_{60}$ and $\mathrm{C}_{70}$ with DMA. By collecting a series of ${ }^{3} \mathrm{He} \mathrm{NMR}$ spectra of reaction mixtures of ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ and ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$ and DMA, we are able to determine the number of DMA residues bound to the fullerene for each peak in the ${ }^{3} \mathrm{He}$ NMR spectra and to identify how many isomers exist in the reaction mixtures. We found one monoadduct, six bis-adducts, eleven tris-adducts, and ten tetrakis-adducts of $\mathrm{C}_{60}(\mathrm{DMA})_{n}$, and one monoadduct, three bis-adducts of $\mathrm{C}_{70^{-}}$ (DMA $)_{n}$ in the equilibrated reaction mixtures. We obtained equilibrium constants for the reactions of $\mathrm{C}_{60}$ and $\mathrm{C}_{70}$ with DMA and the associated $\Delta G, \Delta H$, and $\Delta S$ values.

Acknowledgment. We are grateful to Dr. Anthony Khong for the highly labeled ${ }^{3} \mathrm{He} @ \mathrm{C}_{60}$ sample and to the National Science Foundation for financial support.

JA001346C


[^0]:    ${ }^{\dagger}$ Present address: Dept. of Chemistry, University of Science and Technology of China, Hefei, Anhui 230026, P. R. China.
    (1) Hirsch, A. The Chemistry of Fullerenes; Thieme, Stuttgart, 1994.
    (2) Hirsch, A. Top. Curr. Chem. 1999, 199, 1-65 and references therein.
    (3) Thilgen, C.; Diederich, F. Top. Curr. Chem. 1999, 199, 135-171 and references therein.
    (4) Lamparth, I.; Maichle-Mössmer, C.; Hirsch, A. Angew. Chem., Int. Ed. Engl. 1995, 34, 1607-1609.
    (5) Saunders, M.; Cross, R. J.; Jiménez-Vázquez, H. A.; Shimshi, R.; Khong, A. Science 1996, 271, 1693-1697 and references therein.
    (6) For recent representive literature, see: (a) Cross, R. J.; JimenezVazquez, H. A.; Lu, Q.; Saunders, M.; Schuster, D. I.; Wilson, S. R.; Zhao, H. J. Am. Chem. Soc. 1996, 118, 11454-11459. (b) Ruttimann, M.; Haldimann, R. F.; Isaacs, L.; Diederich, F.; Khong, A.; Jimenez-Vazquez, H. A.; Cross, R. J.; Saunders, M. Chem. Eur. J. 1997, 3, 1071-1076. (c) Shabtai, E.; Weitz, A.; Haddon, R. C.; Hoffman, R. E.; Rabinovitz, M.; Khong, A.; Cross, R. J.; Saunders, M.; Cheng, P.-C.; Scott, L. T. J. Am. Chem. Soc. 1998, 120, 6389-6393. (d) Birkett, P. R.; Buhl, M.; Khong, A.; Saunders, M.; Taylor, R. J. Chem. Soc., Perkin Trans. 2 1999, 20372039.
    (7) Schick, G.; Hirsch, A.; Mauser, H.; Clark, T. Chem. Eur. J. 1996, 2, 935-943.

[^1]:    (8) Djojo, F.; Herzog, A.; Lamparth, I.; Hampel, F.; Hirsch, A. Chem. Eur. J. 1996, 2, 1537-1547.
    (9) (a) Hirsch, A.; Lamparth, I.; Karfunkel, H. R. Angew. Chem., Int. Ed. Engl. 1994, 33, 437-438. (b) Hamano, T.; Mashino, T.; Hirobe, M. Chem. Comтип. 1995, 1537-1538. (c) Issacs, L.; Diederich, F.; Haldimann, R. F. Helv. Chim. Acta 1997, 80, 317-342. (d) Cardullo, F.; Seiler, P.; Issacs, L.; Nierengarten, J.-F.; Haldimann, R. F.; Diederich, F.; MordasiniDenti, T.; Thiel, W.; Bouldon, C.; Gisselbrecht, J.-P.; Gross, M. Helv. Chim. Acta 1997, 80, 343-371. (e) Nierengarten, J.-F.; Habicher, T.; Kessinger, R.; Cardullo, F.; Diederich, F.; Gramlich, V.; Gisselbrecht, J.-P.; Bouldon, C.; Gross, M. Helv. Chim. Acta 1997, 80, 2238-2276. (f) Qian, W.; Rubin, Y. Angew. Chem., Int. Ed. 1999, 38, 2356-2360.

[^2]:    ${ }^{a}$ Chemical shift in ppm relative to dissolved ${ }^{3} \mathrm{He}$ gas. ${ }^{b}$ Fraction in each isomer of the total NMR signal for all isomers with a given number of DMA addends.

[^3]:    (16) Besides ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$ (DMA), the dihelium species ${ }^{3} \mathrm{He}_{2} @ \mathrm{C}_{70}$ (DMA) was also observed at -26.77 ppm . Its intensity is $\sim 10 \%$ of ${ }^{3} \mathrm{He} @ \mathrm{C}_{70}$ (DMA) and the chemical difference is 52 Hz . For a similar observation, see: Khong, A.; Jiménez-Vázquez, H. A.; Saunders, M.; Cross, R. J.; Laskin, J.; Peres, T.; Lifshitz, C.; Strongin, R.; Smith, A. B., III. J. Am. Chem. Soc. 1998, 120, 6380-6383.

